SU(N) Magnetism with Cold Atoms and Chiral Spin Liquids

Victor Gurarie

collaboration with M. Hermele, A.M. Rey



UPC, Barcelona, July 5 2010

In this talk

Alkaline earth atoms can be though of as having SU(N) spins, generalization of the usual SU(2) spins.

► SU(N) magnets are more controllable theoretically than their SU(2) counterparts and have richer phase diagrams

Heisenberg antiferromagnets" of the SU(N) spins can be Chiral Spin Liquids, spins counterparts of quantum Hall effect, states of matter having excitations with fractional and non-Abelian statistics. Those, as is well known, can be used for quantum computation. SU(N) magnetism

LIGHT





Origin of the antiferromagnetism: Mott insulator of spinful electrons





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Cuprates' phase diagram

(occurs when one has close to one electron per lattice site)

 $\hat{H} = -J$ $\sum \hat{f}^{\dagger}_{j,\beta}\hat{f}_{i,\beta}\hat{f}^{\dagger}_{i,\alpha}\hat{f}^{\dagger}_{j,\alpha}$ $\langle ij \rangle; \alpha, \beta = \uparrow, \downarrow$

Origin of the antiferromagnetism: Mott insulator of spinful electrons



spin-up spin-down





Alkaline earth atoms: SU(N) spins

two electrons in the outer shell



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A.V. Gorshkov, M. Hermele, VG, C. Xu, P.S. Julienne, J. Ye, P. Zoller, E. Demler, M.D. Lukin, A.M. Rey. (2010)

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Interesting twist: only fermionic atoms have N>1 (bosons have even-even nuclei, whose I=0)







⁸⁷Sr atoms

 $f_{i,\alpha}^{\dagger}$

Creates an atom on a site i, with nuclear spin α .





Bottom line: these are SU(N) spin antiferromagnets

Experiments with ⁸⁷Sr, SU(10)

Degenerate Fermi Gas of ⁸⁷Sr

B. J. DeSalvo, M. Yan, P. G. Mickelson, Y. N. Martinez de Escobar, and T. C. Killian Rice University, Department of Physics and Astronomy, Houston, Texas, 77251

(Dated: May 6, 2010)

We report quantum degeneracy in a gas of ultra-cold fermionic ⁸⁷Sr atoms. By evaporatively cooling a mixture of spin states in an optical dipole trap for 10.5 s, we obtain samples well into the degenerate regime with $T/T_F = 0.26^{+.05}_{-.06}$. The main signature of degeneracy is a change in the momentum distribution as measured by time-of-flight imaging, and we also observe a decrease in evaporation efficiency below $T/T_F \sim 0.5$.

Double-degenerate Bose-Fermi mixture of strontium



Experiments with ¹⁷³Yb, SU(6)

Realization of $SU(2) \times SU(6)$ Fermi System

Shintaro Taie,^{1,*} Yosuke Takasu,¹ Seiji Sugawa,¹ Rekishu Yamazaki,^{1,2} Takuya Tsujimoto,¹ Ryo Murakami,¹ and Yoshiro Takahashi^{1,2}

¹Department of Physics, Graduate School of Science, Kyoto University, Japan 606-8502 ²CREST, JST, 4-1-8 Honcho Kawaguchi, Saitama 332-0012, Japan (Dated: May 21, 2010)

We report the realization of a novel degenerate Fermi mixture with an $SU(2) \times SU(6)$ symmetry in a cold atomic gas. We successfully cool the mixture of the two fermionic isotopes of ytterbium ¹⁷¹Yb with the nuclear spin I = 1/2 and ¹⁷³Yb with I = 5/2 below the Fermi temperature T_F as $0.46T_F$ for ¹⁷¹Yb and $0.54T_F$ for ¹⁷³Yb. The same scattering lengths for different spin components make this mixture featured with the novel $SU(2) \times SU(6)$ symmetry. The nuclear spin components are separately imaged by exploiting an optical Stern-Gerlach effect. In addition, the mixture is loaded into a 3D optical lattice to implement the $SU(2) \times SU(6)$ Hubbard model. This mixture will open the door to the study of novel quantum phases such as a spinor Bardeen-Cooper-Schrieffer-like fermionic superfluid.

PACS numbers: 03.75.Ss, 67.85.Lm, 37.10.Jk

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FIG. 5. (Color online) Quasimomentum distribution of (a) 171 Yb and (b) 173 Yb in the SU(2)×SU(6) two-species mixture in an optical lattice. The density distributions integrated along the vertical direction are also shown below. The atom numbers are 0.4×10^4 for 171 Yb and 1.5×10^4 for 173 Yb, respectively. The images are taken after linear ramping down of the lattice in 0.5ms, followed by a ballistic expansion of (a) 12ms and (b) 13ms. The dotted lines indicate the domain of the 1st Brillouin zone, which equals twice the recoil momentum $\hbar k$.

SU(N) antiferromagnets

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S. Sachdev

N. Read





I. Affleck J. B. Marston

Late 1980's Careful and numerous studies of the SU(N) antiferromagnets. Papers with many 100's of citations.

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Does this mean we can just look up the answer in these papers and find out all we need to know about SU(N) antiferromagnets and alkaline earth atoms?

NO!

Standard SU(2) antiferromagnet: Néel state



A collection of spin-1/2s on a square lattice in the presence of the antiferromagnetic interactions at T=0 forms a Néel state with a long range antiferromagnetic order (this is known numerically and experimentally).

SU(2) spins: two spins-1/2 can form a singlet



П

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$$\phi_{\uparrow}^{(1)}\phi_{\downarrow}^{(2)} - \phi_{\downarrow}^{(1)}\phi_{\uparrow}^{(2)}$$

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 $lpha,eta=1,2,\ldots,N$

SU(N) spins: at least N spins needed to form a singlet

11

2 spins: $\phi_{\alpha\beta}^{(1,2)} = \phi_{\alpha}^{(1)}\phi_{\beta}^{(2)} - \phi_{\beta}^{(1)}\phi_{\alpha}^{(2)}$ This is not a singlet, but an antisymmetric *N* by *N* tensor, with *N(N-1)/2* components.

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 α, β

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 $\phi_{\alpha\beta\gamma}^{(1,2,3)}$ 3 spins: antisymmetric rank 3 tensor: N(N-1)(N-2)/3! components

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 $\phi^{(1,2,\ldots,N)}_{\alpha_1\alpha_2\ldots\alpha_N}$

N spins: finally, scalar!

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Method: Place *m* and *N-m* spins on even and odd sublattices respectively

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Analytics at large *N*: The ground state is Valence Bond Solid (VBS)

N-m Numerics: the ground state is Néel if N<4 (VBS) VBS if N>4

VBS

5

6

VBS

All of this is not relevant for us: we can place one, at most two atoms (SU(N) spins) on each site

Thus this is a new yet unexplored problem
One atom (or two) per site: experimentally realizable SU(N)



at least *N* (or *N/2*) sites are required to form a singlet

D. Arovas (2008) calls these N-simplexes.



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Large *N* methods

Large N methods

Taking *N* to infinity is problematic: the number of spins required to form a singlet goes to infinity too.

Proposal: Let us put
$$m = \frac{N}{k}$$
 atoms on each site.

The number of sites required to form a singlet is now k and is N independent. Then take N to infinity.

Carrying out this procedure results in the chiral spin liquid ground state if k>4.

M. Hermele, VG, A.-M. Rey (2009)



$$H = -\frac{J}{N} \sum_{\langle ij \rangle, \alpha, \beta = 1, \dots, N} \hat{f}_{j,\beta}^{\dagger} \hat{f}_{i,\beta} \hat{f}_{i,\alpha} \hat{f}_{j,\alpha}$$

Hubbard-Stratonovich hopping

$$S = \int d\tau \left[\sum_{i} \left\{ \sum_{\alpha} \bar{f}_{i,\alpha} \partial_{\tau} f_{i\alpha} + i\lambda_{i} \left(\sum_{\alpha} \bar{f}_{i,\alpha} f_{i,\alpha} - \frac{N}{k} \right) \right\} + \sum_{\langle ij \rangle} \left\{ \chi_{ij} \sum_{\alpha} \bar{f}_{i\alpha} f_{j\alpha} + \text{H.c.} + N \frac{\left| \chi_{ij} \right|^{2}}{J} \right\} \right]$$

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Saddle point equations (exact in the large *N* limit)

$$\frac{1}{k} = \left\langle \hat{f}_{i,\alpha}^{\dagger} \hat{f}_{i,\alpha} \right\rangle \qquad \qquad \chi_{ij} = -J \left\langle \hat{f}_{j,\alpha}^{\dagger} \hat{f}_{i,\alpha} \right\rangle$$

Fermions try to arrange their hopping dynamically to minimize their energy

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Nonzero hopping $\chi^{(0)}$



Spins pair up to form 2-spin singlets This state (VBS) was found by Affleck & Marston in 1989



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Spins pair up to form 2-spin singlets This state (VBS) was found by Affleck & Marston in 1989

Spins form 6-spin Sp singlets (new result)

Spins form 4-spin singlets (new result)

k = 4

Saddle points for k>4

To minimize their energy, fermions attempt to organize hoppings so that they completely fill a band

The filling fraction for fermions with one of N spin components is

$$\nu = \frac{1}{N} \frac{N}{k} = \frac{1}{k}$$

Fermions would like to form a closed band with N_s/k states

Our result: the best way to do that is by arranging a "magnetic flux" of $2\pi/k$ per plaquette and fill the lowest

 $\frac{2\pi/k}{2\pi/k} \frac{2\pi/k}{2\pi/k}$

Landau level.

M. Hermele, VG, A.-M. Rey (2009)

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Chiral Spin Liquid

Chiral Spin Liquid (CSL)





Wen, Wilczek & Zee Kalmeyer & Laughlin Proposed in 1989

A state of magnets without any magnetic order (spin liquid), but breaking parity and time reversal invariance (chiral). Has to be described by a Chern-Simons theory. (Local) Hamiltonians whose ground state would be CSL were unknown until now Chiral spin liquid (k>4)

$$\begin{split} H &= \sum_{\langle ij \rangle, \alpha} \chi_{ij}^{(0)} \left(\hat{f}_{i,\alpha}^{\dagger} \hat{f}_{j,\alpha} + \text{H.c.} \right) \\ & \text{magnetic field with 1/k flux through plaquette} \\ & \text{like quantum Hall effect} \\ & \chi_{ij} = \chi_{ij}^{(0)} e^{iA_{ij}} \\ & S_{\text{eff}} = \frac{N}{4\pi} \int d^2x dt \, \epsilon_{\mu\nu\rho} A_{\mu} \partial_{\nu} A_{\rho} \end{split}$$
 Level N Chern Simons theory

Fermions acquire fractional statistics with the angle θ :

$$\theta = \pi + \frac{\pi}{N} \qquad \qquad N = k, 2k, 3k, \dots$$

Chiral spin liquid (k>4)

$$H = \sum_{\langle ij \rangle, \alpha} \chi_{ij}^{(0)} \left(\hat{f}_{i,\alpha}^{\dagger} \hat{f}_{j,\alpha} + \text{H.c.} \right)$$



magnetic field with 1/k flux through plaquette like quantum Hall effect $\chi_{ij} = \chi_{ij}^{(0)} e^{iA_{ij}}$ $S_{\text{eff}} = \frac{N}{4\pi} \int d^2x dt \,\epsilon_{\mu\nu\rho} A_{\mu} \partial_{\nu} A_{\rho}$ Level N Chern-Simons theory

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$$H = \sum_{\langle ij \rangle, \alpha} \chi_{ij}^{(0)} \left(\hat{f}_{i,\alpha}^{\dagger} \hat{f}_{j,\alpha} + \text{H.c.} \right) \psi(\mathbf{r}_{2}, \psi(\mathbf{r}_{2}, \mathbf{r}_{2}))$$

$$\psi(\mathbf{r}_2,\mathbf{r}_1) = e^{i\left(\pi + \frac{\pi}{N}\right)}\psi(\mathbf{r}_1,\mathbf{r}_2)$$

magnetic field with 1/k flux through plaquette like quantum Hall effect $\chi_{ij} = \chi_{ij}^{(0)} e^{iA_{ij}}$ $S_{\text{eff}} = \frac{N}{4\pi} \int d^2x dt \,\epsilon_{\mu\nu\rho} A_{\mu} \partial_{\nu} A_{\rho}$ Level N Chern-Simons theory

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Who's the carrier of the statistics?

 $\hat{S}^{\alpha}_{\beta}(i) = \hat{f}^{\dagger}_{i,\alpha}\hat{f}_{i,\beta}$ The spin itself is not fractional

The fermions are fractional, but with each site containing exactly one atom, the fermionic atoms don't have any dynamics, fractional or otherwise

Let's create "holes" - empty atomless sites on the lattice $\hat{f}_{i,\alpha} = \hat{b}_i^{\dagger} \hat{c}_{i,\alpha}^{c}$ "spinon" - fermion carrying spin $\hat{f}_{i,\alpha} = \hat{b}_i^{\dagger} \hat{c}_{i,\alpha}^{c}$ "holon" - boson carrying atom number $\hat{f}_{i,\alpha} = \hat{b}_i^{\dagger} \hat{c}_{i,\alpha}^{c}$ "holon" - boson carrying atom number $\hat{f}_{i,\alpha} = \hat{b}_i^{\dagger} \hat{c}_{i,\alpha}^{c}$ "holon" - boson from high T_c theories - only here justified by large N.

Both spinons and holons are fractional, but only holons respond to an external potential

P.A. Lee, N. Nagaosa (1992)

Scenario to create fractional excitations

site potential



Lowering the potential at one site localizes a fractional particle at that site.

localized fractional holon

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Place two species of fermionic atoms on each site, in two distinct electronic states ${}^{1}S_{0}$ and ${}^{3}P_{0}$.

They form either antisymmetric (boring) or <u>symmetric</u> (interesting) state depending on the relative strength of interaction constants (10 author paper)

 $a, b = {}^{1}S_{0}, {}^{3}P_{0}$ labels species

 $|s\rangle = \frac{1}{\sqrt{2}} \left(\hat{f}_{a,\alpha}^{\dagger} \hat{f}_{b,\beta}^{\dagger} + \hat{f}_{b,\alpha}^{\dagger} \hat{f}_{a,\beta}^{\dagger} \right) |0\rangle \text{ on every site of the lattice}$

$$H = \sum_{\langle ij\rangle,a,b,\alpha,\beta} \hat{f}^{\dagger}_{i,a,\alpha} \hat{f}_{i,a,\beta} \hat{f}^{\dagger}_{j,b,\beta} \hat{f}_{j,b,\alpha}$$

Place two species of fermionic atoms on each site, in two distinct electronic states ${}^{1}S_{0}$ and ${}^{3}P_{0}$.

$$H = \sum_{\substack{ij,a,b,\alpha \\ \uparrow \uparrow}} \chi_{ij}^{(0)}{}^{ab} \hat{f}_{i,a,\alpha}^{\dagger} \hat{f}_{j,b,\alpha} \qquad \chi_{ij}^{ab} = \chi_{ij}^{(0)}{}^{ab} e^{iA_{ij}^{ab}}$$

$$a, b = {}^{1}S_{0}, {}^{3}P_{0} \text{ labels species}$$

$$\chi_{ij}^{(0)}{}^{ab} = \delta_{ab}\chi_{ij}^{(0)} \longleftarrow \text{ magnetic field}$$

$$S_{CS} = \frac{N}{4\pi} \text{Tr} \int d^{2}x dt \,\epsilon_{\mu\nu\rho} \left[A_{\mu}\partial_{\nu}A_{\rho} + \frac{2}{3}A_{\mu}A_{\nu}A_{\rho} \right]$$

This is non-Abelian Chern-Simons SU(2)_N theory!

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This is non-Abelian Chern-Simons $SU(2)_N$ theory! Topological quantum computing with $SU(2)_{10}!$ Λ^{ab}_{ij}





A. Kitaev, 1997

Non-Abelian particles are perfect qubits



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A. Kitaev, 1997





Non-Abelian particles are perfect qubits

A. Kitaev, 1997

 $\psi_{\alpha}(\mathbf{r}_{2},\mathbf{r}_{1}) = \sum_{\beta} U_{\alpha,\beta}\psi_{\beta}(\mathbf{r}_{1},\mathbf{r}_{2})$









Welcome!

Welcome to Station Q

People

Research

Station Q is a Microsoft research group working on topological quantum computing. The group combines researchers from math, physics and computer science.

· <u>(onditional</u> or ·test format (see

We wish we had an

SU(2)₂ Pfaffian, p+ip superconductor, all those Majorana fermions...





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How about SU(2)₁₀!





Status of numerics

- Numerical methods are the only way to access the experimentally relevant m=1 column
- QMC sign problem for k>2, at least in 2D
- Other 2D numerical methods?

Conclusions

SU(N) magnets are a useful theoretical construct due to the existence of the large N techniques

SU(N) magnets can have phases going beyond the phases of the SU(2) magnets

Nuclear spin of the alkaline earth atoms a perfect realization of the SU(N) spin - so far lacking in condensed matter

A version of the SU(N) magnets particularly well suited to realization by the alkaline earth atoms forms chiral spin liquids, a state of matter with fractionalized excitations

Possibility of the topological quantum computing with the SU(N) spin magnets??
